PAPER Iterative MMSE Detection with Interference Cancellation for Up-Link HARQ Using Frequency-Domain Filtered SC-FDMA MIMO Multiplexing

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SUMMARY In this paper, we propose an iterative minimum mean square error detection with interference cancellation (MMSED-IC) for frequency-domain filtered single carrier (SC)-frequency-division multipleaccess (FDMA) uplink transmission. The use of a square-root Nyquist transmit filter reduces the peak-to-average power ratio (PAPR) while increases the frequency-diversity gain. However, if carrier-frequency separation among multiple-access users is kept the same as the one used for the case of roll-off factor $\alpha=0$ (i.e., brick-wall filter), then the adjacent users' spectra will overlap and multi-user interference (MUI) occurs. The proposed MMSED-IC can sufficiently suppress the MUI from adjacent users while achieving the maximum frequency-diversity gain. We apply the proposed MMSED-IC to a packet access using filtered SC-FDMA, multi-input multi-output (MIMO) multiplexing, and hybrid automatic repeat request (HARQ). It is shown by computer simulation that filtered SC-FDMA with $\alpha = 1$ can achieve higher throughput than orthogonal frequency division multiple access (OFDMA).

key words: SC-FDMA, MMSED, interference cancellation, frequencydomain filter, MIMO, HARQ

1. Introduction

In the next generation mobile communication systems, broadband packet data services are demanded. Since the broadband wireless channel is composed of many propagation paths with different time delays, the packet error rate (PER) performance degrades due to inter-symbol interference (ISI) arising from the strong frequency-selectivity of the channel [1], [2]. Orthogonal frequency division multiplexing (OFDM) converts the frequency-selective channel into a number of orthogonal frequency-nonselective channels (sub-carriers) and alleviates the ISI problem [3], [4]. However, OFDM has a problem of high peak-to-average power ratio (PAPR) [5]. On the other hand, single-carrier (SC) transmission has low PAPR. The use of minimum mean square error frequency-domain equalization (MMSE-FDE) makes use of the channel frequency-selectivity to improve the PER performance [6]–[8]. SC combined with frequency-division multiple-access (SC-FDMA) [9] has been adopted as the uplink multiple access technique for 3GPP LTE systems [10].

To limit the SC signal bandwidth while reducing the PAPR, square-root Nyquist filters can be used as transmit/receive filters [2], [11]. However, in the 3GPP LTE systems, the ideal brick-wall filter (i.e., a filter of roll-off factor equal to 0) is used for band-limiting each user's transmit signal and the different users' transmit signal spectra are located so as not to overlap each other. As the filter roll-off factor α of the transmit filter increases, the PAPR decreases and furthermore, an additional frequency-diversity gain can be obtained by making use of the excess bandwidth introduced by the transmit filter [12]. However, if the carrierfrequency separation among multiple access users is kept the same as in the case of $\alpha = 0$, the adjacent users' transmit signal spectra are overlapped and the throughput performance degrades due to increased multi-user interference (MUI). In this paper, we call the above SC-FDMA as "filtered SC-FDMA.'

In our previous work [13], we proposed an iterative MMSE-FDE with MUI cancellation (MMSE-FDE/MUIC) for frequency-domain square-root Nyquist transmit filtered uplink SC-FDMA with antenna diversity. In MMSE-FDE/MUIC, joint single-user MMSE-FDE & spectrum combining and MUI cancellation is performed for each user. However, when higher level data modulation (e.g., 16QAM) is used, a big PER performance gap from the single-user case is observed.

In this paper, we propose an iterative MMSE detection with interference cancellation (MMSED-IC) scheme for frequency-domain filtered SC-FDMA uplink transmission. In this scheme, joint MMSE detection and cancellation of MUI, inter-antenna interference (IAI), and ISI is performed iteratively. The proposed MMSED-IC can sufficiently suppress the MUI from adjacent users while achieving the maximum frequency-diversity gain. The proposed MMSED-IC is applied to a frequency-domain filtered SC-FDMA multi-input multi-output (MIMO) multiplexing system.

The remainder of this paper is organized as follows. The frequency-domain filtered SC-FDMA MIMO multiplexing system is presented in Sect. 2. In Sect. 3, we describe the proposed MMSED-IC. In Sect. 4, we evaluate PAPR, PER, and throughput performances by computer simulation. Sect. 5 concludes this paper.

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2. Transmission System Model

The uplink SC-FDMA (N_t, N_r) MIMO multiplexing transmitter/receiver structure is illustrated in Fig. 1. Throughout the paper, fast Fourier transform (FFT) sample-spaced discrete-time signal representation is used. The Chase combining [14] is assumed for packet combining. A total of *U* users are transmitting their data simultaneously.

At the *u*th (u=0,..., U-1) user's transmitter, an information bit sequence is turbo encoded, interleaved, and then transformed into a sequence of data modulated symbols. The data modulated symbol sequence is divided into *M*-symbol each and converted to *N_t* parallel data symbol blocks by a serial/parallel (S/P) converter. Each data symbol block is transformed into the frequency-domain signal of *M* orthogonal subcarriers. Then, the square-root Nyquist filter of roll-off factor α is applied (the signal spectrum is spread over $(1 + \alpha)M$ subcarriers).

The frequency-domain signal after transmit filtering is mapped over $N_c = U \cdot M$ subcarriers. In this paper, we consider the localized mapping illustrated in Fig. 2. The carrier-frequency separation is kept the same as in the case of α =0. The frequency-domain signal after spectrum mapping is transformed back to the time-domain signal by applying an N_c -point inverse FFT (IFFT). Last N_g samples of each block are copied as a cyclic prefix (CP) and inserted into the guard interval (GI) placed at the beginning of each block.

 $U \cdot N_t$ signal blocks are transmitted simultaneously from



Fig. 1 Transmission system model.



Fig. 2 Spectrum mapping.

 N_t transmit antennas. At the BS's n_r th $(n_r=0, ..., N_r-1)$ receive antenna, the received signal block is transformed, after the removal of GI, into the frequency-domain signal by applying an N_c -point FFT. Then, the iterative signal detection is performed $I(\geq 1)$ times for each antenna and each user.

2.1 Transmit Signal Representation

The data symbol block $\mathbf{d}_{u,n_t} = [d_{u,n_t}(0), \dots, d_{u,n_t}(M-1)]^T$ is first transformed by an *M*-point discrete Fourier transform (DFT) into frequency-domain signal $\mathbf{D}_{u,n_t} = [D_{u,n_t}(0), \dots, D_{u,n_t}(M-1)]^T = \mathbf{F}_M \mathbf{d}_{u,n_t}$, to which the transmit filter and localized spectrum mapping are applied. The frequency-domain output $\mathbf{S}_{u,n_t} = [S_{u,n_t}(0), \dots, S_{u,n_t}(N_c-1)]^T$ can be expressed as

$$\mathbf{S}_{u,n_t} = \mathbf{\Phi}_u \mathbf{H}_T \mathbf{D}_{u,n_t},\tag{1}$$

where \mathbf{F}_M is *K*-point DFT matrix given as

$$\mathbf{F}_{K} = \frac{1}{\sqrt{K}} \begin{bmatrix} 1 & 1 & \cdots & 1\\ 1 & e^{\frac{-j2\pi\cdot 1\cdot 1}{K}} & \cdots & e^{\frac{-j2\pi\cdot 1\cdot (K-1)}{K}}\\ \vdots & \vdots & \ddots & \vdots\\ 1 & e^{\frac{-j2\pi\cdot (K-1)\cdot 1}{K}} & \cdots & e^{\frac{-j2\pi\cdot (K-1)\cdot (K-1)}{K}} \end{bmatrix}, \quad (2)$$

and \mathbf{H}_T is the transmit filter matrix of size $2M \times M$, whose (x, y)th $(x=0, \ldots, 2M-1, y=0, \ldots, M-1)$ element $H_T(x, y)$ is given as

$$H_T(x,y) = \begin{cases} f(x-M) & y = (x-M/2) \mod M \\ 0 & otherwise \end{cases}$$
(3)

In this paper, square-root raised cosine Nyquist filter with roll-off factor α is assumed for the transmit filter whose transfer function {f(k); $k = -M \sim M - 1$ } is given by

$$f(k) = \begin{cases} 1 & 0 \le |k| \le \frac{(1-\alpha)}{2}M \\ \cos\left[\frac{\pi}{2\alpha}\left(\frac{|k|}{M} - \frac{1-\alpha}{2}\right)\right] \frac{(1-\alpha)}{2}M \le |k| \le \frac{(1+\alpha)}{2}M \end{cases} (4)$$

$$0 & otherwise$$

 Φ_u is the localized spectrum mapping matrix of size $N_c \times 2M$, whose (x, y)th $(x=0, ..., N_c - 1, y=0, ..., 2M - 1)$ element $\Phi_u(x, y)$ is given as

$$\Phi_u(x,y) = \begin{cases} 1 & x = (y + (u - 1/2)M) \text{mod}N_c \\ 0 & otherwise \end{cases}$$
(5)

An N_c -point IFFT is applied to $\mathbf{S}_{u,n_t} = [S_{u,n_t}(0), \dots, S_{u,n_t}(N_c - 1)]^T$ to obtain the transmit time-domain signal $\mathbf{s}_{u,n_t} = [s_{u,n_t}(0), \dots, s_{u,n_t}(N_c - 1)]^T$ as

$$\mathbf{s}_{u,n_t} = \sqrt{\frac{2E_{s,u}}{T_s}} \mathbf{F}_{N_c}^H \mathbf{S}_{u,n_t},\tag{6}$$

where $E_{s,u}$, T_s and $[.]^H$ denote the symbol energy, symbol duration and the Hermitian transpose operation, respectively.

2.2 Received Signal Representation

We assume that the same packet has been transmitted Q times (i.e., the number of retransmission is Q-1). The propagation channel is assumed to be an *L*-path block fading channel, each path being subjected to independent fading. Let $h_{u,n_l,n_r,l}^{(q)}$ and $\tau_{u,l}$ respectively denote the complex-valued path gain and the delay time of the *l*th path between the *u*th user's n_l th transmit antenna and the BS's n_r th receive antenna for the *q*th (q = 1, ..., Q) packet transmission. The channel impulse response is expressed as

$$h_{u,n_{r},n_{r}}^{(q)}(\tau) = \sum_{l=0}^{L-1} h_{u,n_{r},n_{r},l}^{(q)} \delta(\tau - \tau_{u,l}),$$
(7)

where $\delta(\tau)$ is the delta function. The time delay of each propagation path is assumed to be an integer multiple of the IFFT sampling period. The received signal block on the n_r th received antenna can be expressed using matrix form as

$$\mathbf{r}_{n_r}^{(q)} = \sum_{u=0}^{U-1} \sum_{n_t=0}^{N_t-1} \mathbf{h}_{u,n_t,n_r}^{(q)} \mathbf{s}_{u,n_t} + \mathbf{n}_{n_r}^{(q)},$$
(8)

where $\mathbf{n}_{n_r}^{(q)} = [n_{n_r}^{(q)}(0), \dots, n_{n_r}^{(q)}(N_c - 1)]^T$ is the noise vector with N_c elements being independent zero-mean complex Gaussian variables with variance $2N_0/T_s$ (N_0 is the single-sided power spectrum density of the additive white Gaussian noise (AWGN)) and $\mathbf{h}_{u,n_r,n_r}^{(q)}$ is an $N_c \times N_c$ channel impulse response matrix given as

$$\mathbf{h}_{u,n_{l},n_{r}}^{(q)} = (9)$$

$$\begin{bmatrix} h_{u,n_{l},n_{r},0}^{(q)} & h_{u,n_{l},n_{r},L-1}^{(q)} \cdots & h_{u,n_{l},n_{r},1}^{(q)} \\ \vdots & \ddots & \vdots \\ & & h_{u,n_{l},n_{r},0}^{(q)} & \mathbf{0} & h_{u,n_{l},n_{r},L-1}^{(q)} \\ \\ h_{u,n_{l},n_{r},L-1}^{(q)} & \vdots & \ddots & \\ & \ddots & & \ddots & \\ & \mathbf{0} & h_{u,n_{l},n_{r},L-1}^{(q)} & \cdots & \cdots & h_{u,n_{l},n_{r},0}^{(q)} \end{bmatrix}$$

An N_c -point FFT is applied to $\mathbf{r}_{n_r}^{(q)} = [r_{n_r}^{(q)}(0), \dots, r_{n_r}^{(q)}(N_c-1)]^T$ to transform it into the frequency-domain signal as

$$\mathbf{R}_{n_{r}}^{(q)} = [\mathbf{R}_{n_{r}}^{(q)}(0), \dots, \mathbf{R}_{n_{r}}^{(q)}(N_{c}-1)]^{T}$$

= $\mathbf{F}_{N_{c}}\mathbf{r}_{n_{r}}^{(q)} = \mathbf{F}_{N_{c}}\sum_{u=0}^{U-1}\sum_{n_{t}=0}^{N_{t}-1}\mathbf{h}_{u,n_{t},n_{r}}^{(q)}\mathbf{s}_{u,n_{t}} + \mathbf{F}_{N_{c}}\mathbf{n}_{n_{r}}^{(q)}.$ (10)

Since $\mathbf{h}_{u,n_r,n_r}^{(q)}$ is a circulant matrix,

$$\mathbf{F}_{N_c} \mathbf{h}_{u,n_t,n_r}^{(q)} \mathbf{F}_{N_c}^{H} = \mathbf{H}_{u,n_t,n_r}^{(q)}$$

= diag[$H_{u,n_t,n_r}^{(q)}(0), \dots, H_{u,n_t,n_r}^{(q)}(N_c - 1)$], (11)

and therefore, Eq. (10) can be rewritten as

$$\mathbf{R}_{n_r}^{(q)} = \sum_{u=0}^{U-1} \sum_{n_t=0}^{N_t-1} \sqrt{\frac{2E_{s,u}}{T_s}} \bar{\mathbf{H}}_{u,n_t,n_r}^{(q)} \mathbf{D}_{u,n_t} + \mathbf{N}_{n_r}^{(q)},$$
(12)

where $\mathbf{\bar{H}}_{u,n_t,n_r}^{(q)}$ is equivalent channel matrix given by $\mathbf{\bar{H}}_{u,n_t,n_r}^{(q)} = \mathbf{H}_{u,n_t,n_r}^{(q)} \mathbf{\Phi}_u \mathbf{H}_T$ and $\mathbf{N}_{n_r}^{(q)} = [N_{n_r}^{(q)}(0), \dots, N_{n_r}^{(q)}(N_c - 1)]^T$ is frequency-domain noise vector at the n_r th receive antenna.

Totally of QN_rN_c signal blocks have been received. They can be expressed using vector **R** of size $QN_rN_c \times 1$ as

$$\mathbf{R} = \left[(\mathbf{R}_0^{(1)})^T \dots (\mathbf{R}_{N_r-1}^{(1)})^T \dots (\mathbf{R}_0^{(Q)})^T \dots (\mathbf{R}_{N_r-1}^{(Q)})^T \right]^T$$
$$= \sum_{u=0}^{U-1} \sum_{n_t=0}^{N_t-1} \sqrt{\frac{2E_{s,u}}{T_s}} \bar{\mathbf{H}}_{u,n_t} \mathbf{D}_{u,n_t} + \mathbf{N},$$
(13)

where $\mathbf{\tilde{H}}_{u,n_{t}} = \left[(\mathbf{\tilde{H}}_{u,n_{t},0}^{(1)})^{T} \dots (\mathbf{\tilde{H}}_{u,n_{t},N_{r}-1}^{(1)})^{T} \dots (\mathbf{\tilde{H}}_{u,n_{t},0}^{(Q)})^{T} \dots (\mathbf{\tilde{H}}_{u,n_{t},0}^{(Q)})^{T} \dots (\mathbf{\tilde{H}}_{u,n_{t},0}^{(Q)})^{T} \right]^{T}$ is the equivalent channel matrix of size $QN_{r}N_{c} \times M$.

3. Iterative MMSED with Interference Cancellation

Adjacent users signal spectra are partially overlapped with the desired user due to transmit filtering. In MIMO multiplexing, N_t transmitted signals share the same bandwidth. The proposed iterative MMSED-IC separates the overlapped spectra and restores the frequency-domain signal transmitted from each user's each antenna by using spectrum combining.

The frequency-domain signal $\hat{\mathbf{D}}_{u,n_t}^{(i)} = [\hat{D}_{u,n_t}^{(i)}(0), \dots, \hat{D}_{u,n_t}^{(i)}(M-1)]^T$, which corresponds to \mathbf{D}_{u,n_t} , after MMSED at the *i*th $(i=0,\dots,I-1)$ iteration is given as

$$\begin{split} \hat{\mathbf{D}}_{u,n_{t}}^{(i)} &= \mathbf{W}_{u,n_{t}}^{(i)} \mathbf{R} \\ &= \sqrt{\frac{2E_{s,u}}{T_{s}}} \mathbf{D}_{u,n_{t}} + \sqrt{\frac{2E_{s,u}}{T_{s}}} \left(\mathbf{W}_{u,n_{t}}^{(i)} \bar{\mathbf{H}}_{u,n_{t}} - \mathbf{I} \right) \mathbf{D}_{u,n_{t}} \\ &+ \mathbf{W}_{u,n_{t}}^{(i)} \left(\sum_{u'=0 \neq u}^{U-1} \sum_{n_{t}'=0}^{N_{t}-1} \sqrt{\frac{2E_{s,u'}}{T_{s}}} \bar{\mathbf{H}}_{u',n_{t}'} \mathbf{D}_{u',n_{t}'} \right) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)} \left(\sqrt{\frac{2E_{s,u}}{T_{s}}} \sum_{n_{t}'=0 \neq n_{t}}^{N_{t}-1} \bar{\mathbf{H}}_{u,n_{t}'} \mathbf{D}_{u,n_{t}'} \right) + \mathbf{W}_{u,n_{t}}^{(i)} \mathbf{N}, \end{split}$$
(14)

where $\mathbf{W}_{u,n_t}^{(i)}$ is the MMSE weight matrix of size $M \times QN_r N_c$.

The receiver structure with MMSED-IC is illustrated in Fig. 3. In this paper, we apply parallel IC (PIC). Frequencydomain MUI, IAI, and ISI cancellation is carried out simultaneously as



Fig. 3 Receiver structure with iterative MMSED-IC.

$$\check{\mathbf{D}}_{u,n_t}^{(i)} = \hat{\mathbf{D}}_{u,n_t}^{(i)} - \tilde{\mathbf{M}}_{u,n_t}^{(i)} - \tilde{\mathbf{A}}_{u,n_t}^{(i)} - \tilde{\mathbf{I}}_{u,n_t}^{(i)},$$
(15)

where $\tilde{\mathbf{M}}_{u,n_t}^{(i)}$, $\tilde{\mathbf{A}}_{u,n_t}^{(i)}$ and $\tilde{\mathbf{I}}_{u,n_t}^{(i)}$ are respectively the MUI, IAI and ISI replicas which will be shown in 3.1. $\mathbf{W}_{u,n_t}^{(i)}$ in Eq. (14) is the MMSE weight matrix which minimizes the trace of the covariance matrix $E\left[(\mathbf{e}_{u,n_t}^{(i)})(\mathbf{e}_{u,n_t}^{(i)})^H\right]$ of the error vector between $\mathbf{D}_{u,n_t}^{(i)}$ (the transmitted block) and $\check{\mathbf{D}}_{u,n_t}^{(i)}$.

The soft decision symbol $\check{\mathbf{d}}_{u,n_t}^{(i)} = [\check{d}_{u,n_t}^{(i)}(0), \dots, \check{d}_{u,n_t}^{(i)}(M-1)]^T$ is obtained by applying an *M*-point IDFT to $\check{\mathbf{D}}_{u,n_t}^{(i)} = [\check{D}_{u,n_t}^{(i)}(0), \dots, \check{D}_{u,n_t}^{(i)}(M-1)]^T$ as

$$\check{\mathbf{d}}_{u,n_t}^{(i)} = \mathbf{F}_M^H \check{\mathbf{D}}_{u,n_t}^{(i)}.$$
(16)

3.1 Generation of $\tilde{\mathbf{M}}_{u,n_t}^{(i)}, \tilde{\mathbf{A}}_{u,n_t}^{(i)}$, and $\tilde{\mathbf{I}}_{u,n_t}^{(i)}$

The soft symbol replica $\{\tilde{d}_{u,n_t}^{(i)}(m)\}$ is given as [15]

$$\begin{split} \tilde{d}_{u,n_{t}}^{(i-1)}(m) &= \\ \left\{ \frac{1}{\sqrt{2}} \tanh\left(\frac{\lambda_{0,u,n_{t}}^{(i-1)}(m)}{2}\right) + j\frac{1}{\sqrt{2}} \tanh\left(\frac{\lambda_{1,u,n_{t}}^{(i-1)}(m)}{2}\right) \right\} \text{forQPSK} \\ \left\{ \frac{1}{\sqrt{10}} \tanh\left(\frac{\lambda_{0,u,n_{t}}^{(i-1)}(m)}{2}\right) \right\} \left\{ 2 + \tanh\left(\frac{\lambda_{1,u,n_{t}}^{(i-1)}(m)}{2}\right) \right\} \\ + j\frac{1}{\sqrt{10}} \tanh\left(\frac{\lambda_{2,u,n_{t}}^{(i-1)}(m)}{2}\right) \left\{ 2 + \tanh\left(\frac{\lambda_{3,u,n_{t}}^{(i-1)}(m)}{2}\right) \right\} \text{for16QAM} \end{split}$$
(17)

where $\lambda_{x,u,n_t}^{(i-1)}(m)$ is the log-likelihood ratio (LLR) of the *x*th $(x=0,\ldots,N-1)$ bit in the *m*th symbol in a block (*N* is the number of bits per symbol and $m=0,\ldots,M-1$). $\lambda_{x,u,n_t}^{(i-1)}(m)$ is given as

$$\lambda_{x,u,n_{t}}^{(i-1)}(m) = \ln \left(\frac{p_{u,n_{t}}^{(i-1)}(b_{m,x}=1)}{p_{u,n_{t}}^{(i-1)}(b_{m,x}=0)} \right) \\ \approx \frac{\left| \breve{d}_{u,n_{t}}^{(i-1)}(m) - \sqrt{\frac{2E_{s,u}}{T_{s}}} d_{b_{m,x}=0}^{\min} \right|^{2}}{2\left(\hat{\sigma}_{u,n_{t}}^{(i-1)}\right)^{2}} \\ - \frac{\left| \breve{d}_{u,n_{t}}^{(i-1)}(m) - \sqrt{\frac{2E_{s,u}}{T_{s}}} d_{b_{m,x}=1}^{\min} \right|^{2}}{2\left(\hat{\sigma}_{u,n_{t}}^{(i-1)}\right)^{2}}, \quad (18)$$

where $p_{u,n_t}^{(i-1)}(b_{m,x}=0)$ and $p_{u,n_t}^{(i-1)}(b_{m,x}=1)$ are the *a posteriori* probabilities of the transmitted bit $b_{m,x}$ being $b_{m,x}=0$ and $b_{m,x}=1$, respectively, at the (i-1)th iteration stage, $d_{b_{m,x}=0}^{\min}$ (or $d_{b_{m,x}=1}^{\min}$) is the symbol which has the shortest Euclidean distance from $\check{d}_{u,n_t}^{(i-1)}(m)$ and whose *x*th bit is 0 (or 1) and $2\left(\hat{\sigma}_{u,n_t}^{(i-1)}\right)^2$ is the sum of the variances of the MUI, IAI, ISI, and noise.

The soft decision symbol replica block $\tilde{\mathbf{d}}_{u,n_t}^{(i-1)} = [\tilde{d}_{u,n_t}^{(i-1)}(0), \dots, \tilde{d}_{u,n_t}^{(i-1)}(M-1)]^T$ is transformed into the frequency domain signal $\tilde{\mathbf{D}}_{u,n_t}^{(i-1)} = [\tilde{D}_{u,n_t}^{(i-1)}(0), \dots, \tilde{D}_{u,n_t}^{(i-1)}(M-1)]^T$ by applying an *M*-point DFT as

$$\tilde{\mathbf{D}}_{u,n_t}^{(i-1)} = \mathbf{F}_M \tilde{\mathbf{d}}_{u,n_t}^{(i-1)},\tag{19}$$

where $\tilde{d}_{u,n_t}^{(-1)}(m) = 0$. The frequency-domain MUI replica $\tilde{\mathbf{M}}_{u,n_t}^{(i)} = [\tilde{M}_{u,n_t}^{(i)}(0), \dots, \tilde{M}_{u,n_t}^{(i)}(M-1)]^T$, IAI replica $\tilde{\mathbf{A}}_{u,n_t}^{(i)} = [\tilde{A}_{u,n_t}^{(i)}(0), \dots, \tilde{A}_{u,n_t}^{(i)}(M-1)]^T$ and residual ISI replica $\tilde{\mathbf{I}}_{u,n_t}^{(i)} = [\tilde{I}_{u,n_t}^{(i)}(0), \dots, \tilde{I}_{u,n_t}^{(i)}(M-1)]^T$ are generated as

$$\tilde{\mathbf{M}}_{u,n_{t}}^{(i)} = \mathbf{W}_{u,n_{t}}^{(i)} \left(\sum_{u'=0\neq u}^{U-1} \sum_{n_{t}'=0}^{N_{t}-1} \sqrt{\frac{2E_{s,u'}}{T_{s}}} \bar{\mathbf{H}}_{u',n_{t}'} \tilde{\mathbf{D}}_{u',n_{t}'}^{(i-1)} \right), \quad (20)$$

$$\tilde{\mathbf{A}}_{u,n_{t}}^{(i)} = \sqrt{\frac{2E_{s,u}}{T_{s}}} \mathbf{W}_{u,n_{t}}^{(i)} \left(\sum_{n_{t}'=0\neq n_{t}}^{N_{t}-1} \tilde{\mathbf{H}}_{u,n_{t}'} \tilde{\mathbf{D}}_{u,n_{t}'}^{(i-1)} \right),$$
(21)

$$\tilde{\mathbf{I}}_{u,n_t}^{(i)} = \sqrt{\frac{2E_{s,u}}{T_s}} \left(\mathbf{W}_{u,n_t}^{(i)} \bar{\mathbf{H}}_{u,n_t} - \mathbf{I} \right) \tilde{\mathbf{D}}_{u,n_t}^{(i-1)}.$$
(22)

Simultaneous cancellation of MUI, IAI, and residual ISI is carried out according to Eq. (15).

3.2 Derivation of $\mathbf{W}_{u,n_t}^{(i)}$

The error vector $\mathbf{e}_{u,n_t}^{(i)}$ between the frequency-domain signal after interference cancellation $\mathbf{\breve{D}}_{u,n_t}^{(i)}$ and the transmit frequency-domain signal \mathbf{D}_{u,n_t} is defined as

$$\begin{aligned} \mathbf{e}_{u,n_{t}}^{(i)} &= [e_{u,n_{t}}^{(i)}(0), \dots, e_{u,n_{t}}^{(i)}(M-1)]^{T} \\ &= \mathbf{\breve{D}}_{u,n_{t}}^{(i)} - \sqrt{\frac{2E_{s,u}}{T_{s}}} \mathbf{D}_{u,n_{t}} \\ &= \sqrt{\frac{2E_{s,u}}{T_{s}}} \left(\mathbf{W}_{u,n_{t}}^{(i)} \mathbf{\breve{H}}_{u,n_{t}} - \mathbf{I} \right) \left(\mathbf{D}_{u,n_{t}} - \mathbf{\breve{D}}_{u,n_{t}}^{(i-1)} \right) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)} \left(\sum_{u'=0 \neq u}^{U-1} \sum_{n_{t}'=0}^{N_{t}-1} \sqrt{\frac{2E_{s,u'}}{T_{s}}} \mathbf{\breve{H}}_{u',n_{t}'} \left(\mathbf{D}_{u',n_{t}'} - \mathbf{\breve{D}}_{u',n_{t}'}^{(i-1)} \right) \right) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)} \left(\sqrt{\frac{2E_{s,u}}{T_{s}}} \sum_{n_{t}'=0 \neq n_{t}}^{N_{t}-1} \mathbf{\breve{H}}_{u,n_{t}'} \left(\mathbf{D}_{u,n_{t}'} - \mathbf{\breve{D}}_{u,n_{t}'}^{(i-1)} \right) \right) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)} \mathbf{N}. \end{aligned}$$
(23)

MMSE weight is the one which minimizes the trace of the covariance matrix of the error vector as

$$\mathbf{W}_{u,n_{t}}^{(i)} = \arg\min trE\left[\mathbf{e}_{u,n_{t}}^{(i)}\left(\mathbf{e}_{u,n_{t}}^{(i)}\right)^{H}\right]$$

= $\arg\min trE\left[\left(\mathbf{D}_{u,n_{t}} - \tilde{\mathbf{D}}_{u,n_{t}}^{(i-1)}\right)\left(\mathbf{D}_{u,n_{t}} - \tilde{\mathbf{D}}_{u,n_{t}}^{(i-1)}\right)^{H}\right].$ (24)

By solving $\partial tr E \left[\mathbf{e}_{u,n_t}^{(i)} \left(\mathbf{e}_{u,n_t}^{(i)} \right)^H \right] / \partial \mathbf{W}_{u,n_t}^{(i)} = 0$, the MMSE weight at the *i*th stage is given by

$$\mathbf{W}_{u,n_{t}}^{(i)} = E_{s,u}\rho_{u,n_{t}}^{(i-1)} \left(\bar{\mathbf{H}}_{u,n_{t}}\right)^{H} \\ \times \left[\sum_{u'=0}^{U-1} E_{s,u'}\sum_{n_{t}'=0}^{N_{t}-1} \rho_{u',n_{t}'}^{(i-1)} \bar{\mathbf{H}}_{u',n_{t}'} \left(\bar{\mathbf{H}}_{u',n_{t}'}\right)^{H} + N_{0}\mathbf{I}\right]^{-1}, \quad (25)$$

where $\rho_{u,n_t}^{(i)}$ is given as [15]

$$\rho_{u,n_t}^{(i)} = E\left[\left|D_{u,n_t}(k) - \tilde{D}_{u,n_t}^{(i)}(k)\right|^2\right]$$

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$$\approx \frac{1}{M} \sum_{m=0}^{M-1} \left(E[|d_{u,n_t}(m)|^2] - |\tilde{d}_{u,n_t}^{(i)}(m)|^2 \right).$$
(26)

In the above equation, $E[|d_{u,n_t}(m)|^2]$ is the expectation of the transmitted *m*th symbol using the *a posteriori* probability of the transmitted symbols for the given received signal **R** and is given by [15]

$$E[|d_{u}(n)|^{2}] =$$

$$\begin{cases} 1 & \text{for QPSK} \\ \frac{4}{10} \tanh\left(\frac{\lambda_{1,u,n}^{(i-1)}(m)}{2}\right) + \frac{4}{10} \tanh\left(\frac{\lambda_{3,u,n}^{(i-1)}(m)}{2}\right) + 1 & \text{for 16QAM} \end{cases}$$
(27)

Since $\tilde{\mathbf{H}}_{u,n_t}$ in Eq. (25) includes the transfer function of the transmit filter, the MMSE weight also takes the role of a receive filter matched to the transmit filter. $\bar{\mathbf{H}}_{u',n'_t}$ is the equivalent channel matrix of size $QN_rN_c \times M$, and therefore, the matrix inversion in Eq. (25) requires a computational complexity of $O((QN_rN_c)^3)$. In the next subsection, we will propose a reduced complexity MMSE weight computation.

3.3 Reduced Complexity MMSE Weight Computation

The minimization of the trace $trE\left[\mathbf{e}_{u,n_t}^{(i)}(\mathbf{e}_{u,n_t}^{(i)})^H\right]$ is equivalent to the minimization of the squared error $|e_{u,n_t}^{(i)}(k)|$ for $k = 0 \sim M - 1$ since $trE\left[\mathbf{e}_{u,n_t}^{(i)}(\mathbf{e}_{u,n_t}^{(i)})^H\right] = \sum_{k=0}^{M-1} |e_{u,n_t}^{(i)}(k)|^2$.

By interchanging the elements $R_{n_r}^{(q)}(k)$, $\mathbf{R}_{n_r}^{(q)}$ can be transformed into a block-diagonal matrix as

$$\mathbf{R}'_{n_{r}}^{(q)} = \begin{bmatrix} (\mathbf{R}_{n_{r}}^{(q)}(0))^{T} \dots (\mathbf{R}_{n_{r}}^{(q)}(M-1))^{T} \end{bmatrix}^{T} \\ = \begin{bmatrix} \bar{\mathbf{H}}_{n_{r}}^{(q)}(0) & \mathbf{0} \\ \bar{\mathbf{H}}_{n_{r}}^{(q)}(1) & \\ & \ddots & \\ \mathbf{0} & \bar{\mathbf{H}}_{n_{r}}^{(q)}(M-1) \end{bmatrix} \begin{bmatrix} \mathbf{D}(0) \\ \mathbf{D}(1) \\ \vdots \\ \mathbf{D}(M-1) \end{bmatrix} \\ + \mathbf{N}'_{n_{r}}^{(q)}, \qquad (28)$$

where $\mathbf{R}_{n_r}^{(q)}(k)$ is the received signal vector of size $U \times 1$ after spectrum de-mapping, $\mathbf{\bar{H}}_{n_r}^{(q)}(k)$ is the equivalent channel matrix of size $U \times UN_t$, given as

$$\mathbf{R}_{n_{r}}^{(q)}(k) = \mathbf{G}(k)\mathbf{R}_{n_{r}}^{(q)}$$
(29)
= $\left[R_{n_{r}}^{(q)}(k), \dots, R_{n_{r}}^{(q)}(k+xM), \dots, R_{n_{r}}^{(q)}(k+(U-1)M)\right]^{T},$
 $\mathbf{\bar{H}}_{n_{r}}^{(q)}(k) =$ (30)
 $\left[\mathbf{\bar{H}}_{0,0,n_{r}}^{(q)}(k) \dots \mathbf{\bar{H}}_{0,N_{r}-1,n_{r}}^{(q)}(k) \dots \mathbf{\bar{H}}_{U-1,0,n_{r}}^{(q)}(k) \dots \mathbf{\bar{H}}_{U-1,N_{r}-1,n_{r}}^{(q)}(k)\right],$
 $\mathbf{D}(k) =$ (31)
 $\left[D_{0,0}(k), \dots, D_{0,N_{r}-1}(k), \dots, D_{U-1,0}(k), \dots, D_{U-1,N_{r}-1}(k)\right]^{T},$

where G(k) is the spectrum de-mapping matrix of size $U \times N_c$, whose (x, y)th $(x=0, \ldots, U-1, y=0, \ldots, N_c-1)$ element $G_{xy}(k)$ being given as

$$G_{xy}(k) = \begin{cases} 1 & y - k = xM \\ 0 & otherwise \end{cases}$$
(32)

Since the channel matrix in Eq. (28) is block diagonal, Eq. (28) can be rewritten as

$$\begin{aligned} \mathbf{R}_{n_{r}}^{(q)}(k) &= \mathbf{G}(k)\mathbf{R}_{n_{r}}^{(q)} \\ &= \bar{\mathbf{H}}_{n_{r}}^{(q)}(k)\mathbf{D}(k) + \mathbf{N}_{n_{r}}^{(q)}(k) \\ &= \sum_{u=0}^{U-1}\sum_{n_{r}=0}^{N_{r}-1}\sqrt{\frac{2E_{s,u}}{T_{s}}}\bar{\mathbf{H}}_{u,n_{r},n_{r}}^{(q)}(k)D_{u,n_{r}}(k) + \mathbf{N}_{n_{r}}^{(q)}(k), \end{aligned}$$
(33)

where $\bar{\mathbf{H}}_{u,n_t,n_r}^{(q)}(k)$ is the equivalent channel matrix of size $U \times 1$, given as

$$\bar{\mathbf{H}}_{u,n_t,n_r}^{(q)}(k) = \mathbf{G}(k)\bar{\mathbf{H}}_{u,n_t,n_r}^{(q)}\mathbf{C}(k),$$
(34)

with C(k) being an $U \times 1$ vector whose *k*th element is 1 and the others are 0.

It can be shown that the *k*th frequency component $D_{u,n_t}(k)$ transmitted from the n_t th antenna of the *u*th user appears only in $\mathbf{R}_{n_r}^{(q)}(k)$. Thus, it is sufficient to consider $\mathbf{R}_{n_r}^{(q)}(k)$ for the estimation of $D_{u,n_t}(k)$. All the received signal vector $\mathbf{R}(k)$ is written as

$$= \left[\left(\mathbf{R}_{0}^{(1)}(k) \right)^{T} \dots \left(\mathbf{R}_{N_{r}-1}^{(1)}(k) \right)^{T} \dots \left(\mathbf{R}_{0}^{(Q)}(k) \right)^{T} \dots \left(\mathbf{R}_{N_{r}-1}^{(Q)}(k) \right)^{T} \right]^{T}$$
$$= \sum_{u=0}^{U-1} \sum_{n_{t}=0}^{N_{t}-1} \sqrt{\frac{2E_{s,u}}{T_{s}}} \bar{\mathbf{H}}_{u,n_{t}}(k) D_{u,n_{t}}(k) + \mathbf{N}(k), \qquad (35)$$

where $\mathbf{\tilde{H}}_{u,n_t}(k) = \left[\left(\mathbf{\tilde{H}}_{u,n_t,0}^{(1)}(k)\right)^T \dots \left(\mathbf{\tilde{H}}_{u,n_t,N_r-1}^{(1)}(k)\right)^T \dots \left(\mathbf{\tilde{H}}_{u,n_t,0}^{(Q)}(k)\right)^T$ $\dots \left(\mathbf{\tilde{H}}_{u,n_t,N_{r-1}}^{(Q)}(k)\right)^T\right]^T$ is a $QN_rU \times 1$ channel matrix for the *u*th user's n_r th transmit antenna.

MMSE estimation is performed as

$$\begin{split} \hat{D}_{u,n_{t}}^{(i)}(k) &= \mathbf{W}_{u,n_{t}}^{(i)}(k)\mathbf{R}(k) \\ &= \sqrt{\frac{2E_{s,u}}{T_{s}}} D_{u,n_{t}}(k) \\ &+ \sqrt{\frac{2E_{s,u}}{T_{s}}} \left(\mathbf{W}_{u,n_{t}}^{(i)}(k) \bar{\mathbf{H}}_{u,n_{t}}(k) - 1 \right) D_{u,n_{t}}(k) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)}(k) \left(\sum_{u'=0 \neq u}^{U-1} \sum_{n'_{t}=0}^{N_{t}-1} \sqrt{\frac{2E_{s,u'}}{T_{s}}} \bar{\mathbf{H}}_{u',n'_{t}}(k) D_{u',n'_{t}}(k) \right) \quad (36) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)}(k) \left(\sqrt{\frac{2E_{s,u}}{T_{s}}} \sum_{n'_{t}=0 \neq n_{t}}^{N_{t}-1} \bar{\mathbf{H}}_{u,n'_{t}}(k) D_{u,n'_{t}}(k) \right) \\ &+ \mathbf{W}_{u,n_{t}}^{(i)}(k) \mathbf{N}(k), \end{split}$$

where $\mathbf{W}_{u,n_t}^{(i)}(k)$ is the MMSED weight matrix of size $1 \times QN_r U$ which minimizes the MSE $E\left[|e_{u,n_t}^{(i)}(k)|^2\right]$ between $D_{u,n_t}(k)$ (the *k*th frequency component of the transmitted symbol block) and $\check{D}_{u,n_t}^{(i)}(k)$ (the *k*th frequency component of the soft decision symbol block after interference cancellation), given as

$$\mathbf{W}_{u,n_{t}}^{(i)}(k) = E_{s,u} \rho_{u,n_{t}}^{(i-1)} \left(\bar{\mathbf{H}}_{u,n_{t}}(k) \right)^{H}$$

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$$\times \left[\sum_{u'=0}^{U-1} E_{s,u'} \sum_{n_t'=0}^{N_t-1} \rho_{u',n_t'}^{(i-1)} \bar{\mathbf{H}}_{u',n_t'}(k) \left(\bar{\mathbf{H}}_{u',n_t'}(k) \right)^H + N_0 \mathbf{I} \right]^{-1}$$
(37)

It can be understood from Eq. (37) that the inverse matrix computation has an order of $O((QN_rU)^3)$.

The *k*th frequency-domain MUI replica $\tilde{M}_{u,n_t}^{(i)}(k)$, IAI replica $\tilde{A}_{u,n_t}^{(i)}(k)$ and residual ISI replica $\tilde{I}_{u,n_t}^{(i)}(k)$ are generated as

$$\tilde{M}_{u,n_{t}}^{(i)}(k) = \mathbf{W}_{u,n_{t}}^{(i)}(k) \left(\sum_{u'=0 \neq u n_{t}'=0}^{N_{t}-1} \sqrt{\frac{2E_{s,u'}}{T_{s}}} \bar{\mathbf{H}}_{u',n_{t}'}(k) \tilde{D}_{u',n_{t}'}^{(i-1)}(k) \right), \quad (38)$$

$$\tilde{A}_{u,n_{t}}^{(i)}(k) = \sqrt{\frac{2E_{s,u}}{T_{s}}} \mathbf{W}_{u,n_{t}}^{(i)}(k) \left(\sum_{n_{t}'=0\neq n_{t}}^{N_{t}-1} \bar{\mathbf{H}}_{u,n_{t}'}(k) \tilde{D}_{u,n_{t}'}^{(i-1)}(k) \right),$$
(39)

$$\tilde{I}_{u,n_t}^{(i)}(k) = \sqrt{\frac{2E_{s,u}}{T_s}} \left(\mathbf{W}_{u,n_t}^{(i)}(k) \bar{\mathbf{H}}_{u,n_t}(k) - 1 \right) \tilde{D}_{u,n_t}^{(i-1)}(k).$$
(40)

4. Computer Simulation

The simulation condition is summarized in Table 1. A packet access using filtered SC-FDMA, (N_t, N_r) MIMO multiplexing, and HARQ is considered. Chase combining [14] is assumed for packet combining. The number of symbols per block is M=64. QPSK and 16QAM data modulations are considered. The information bit sequence length is 1530 bits. A turbo encoder with two (13,15) RSC encoders and a turbo decoder with Log-MAP algorithm are used. The turbo encoder produces the systematic bit sequence (the information bit sequence) and two parity bit sequences. Therefore, an original coding rate is 1/3. To increase the coding rate to 1/2 and 3/4, the two parity bit sequences are punctured.

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Table I Simulation condition.								
	No. of information bits	1530 (=1packet)						
Channel coding	Encoder	(13,15)RSC						
	Coding rate	R = 1/2, 3/4						
	Channel interleaver	Block						
	Packet combining	Chase combining						
	Decoder	Log-MAP						
Numbers o	f Tx and Rx antennas	$N_t = N_r = 4$						
Transmitter	Data modulation	QPSK, 16QAM						
	No. of symbols per block	M = 64						
	FFT/IFFT size	$N_c = 256$						
	No. of users	$U = 4 \left(= N_c / M\right)$						
	CP length	$N_g = 32$ samples						
Transmit filter	Transfer function	Square-root raised cosine						
	Roll-off factor	$\alpha = 0 \sim 1$						
Channel	Fading type	Frequency-selective						
	Pading type	block Rayleigh						
	Power delay profile	L = 16-path exponential						
	Tower delay profile	power delay profile						
	Decay factor	$\beta = 0, 3 \mathrm{dB}$						
	Time delay	$\tau_{u,l} = l, l = 0 \sim L - 1$						
Receiver	Signal detection	MMSED-IC						
	No. of iterations, I	20 times at the most						
	Channel estimation	Ideal						

The propagation channel for each pair of transmit and receive antennas is assumed to be an *L*=16-path frequency-selective block Rayleigh fading channel having the exponential power delay profile with the decay factor β . No correlation among the propagation paths is assumed. We perform *I* times iterations which is big enough to obtain a sufficient PER improvement but 20 times at the most. The transmit timing is asynchronous among different users, but it is assumed to be kept within the GI. Ideal channel estimation and ideal slow transmit power control ($E_{s,u}=E_s$ for all user) are also assumed.

4.1 PAPR

PAPR is defined as [9]

$$PAPR = \frac{\max\left\{|s_{u,n_t}(t)|^2\right\}_{t=0\sim N_c-1}}{E\left[|s_{u,n_t}(t)|^2\right]}.$$
(41)

The PAPR level in dB at the complementary cumulative distribution function (CCDF)= 10^{-3} is shown in Table 2 for various values of the roll-off factor α [13]. As α increases, the PAPR_{0.1%} level decreases, but it becomes almost the same beyond $\alpha = 0.5$.

4.2 Achievable PER Performance Using Proposed Scheme

No packet retransmission & combining is considered (i.e., Q=1). The PER performance is plotted in Fig. 4 as a function of the average received symbol energy-to-AWGN noise power spectrum density ratio E_s/N_0 when the roll-off factor $\alpha = 0$ and 1. The dacay factor $\beta = 0$ (corresponding to the uniform power delay profile) is assumed. For comparison, the performance without IC (note that 20 decoding iterations are performed in the turbo decoder) is also plotted.

The proposed MMSED-IC improves the PER performance compared with w/o IC since it can suppress the interference (MUI&IAI&ISI) while achieving a higher frequency-diversity and coding gains. In the case of no IC, the PER performance when α =1 degrades compared to when α =0 since larger MUI is present. However, by the use of MMSED-IC, α =1 provides better PER performance. This is because the additional frequency-diversity gain can be obtained by exploiting the excess bandwidth introduced by the transmit filtering.

4.3 Throughput Performance

One packet consists of 1530 information bits. Each user is allocated $(1 + \alpha)M$ subcarriers. However, by allowing the spectrum overlapping between adjacent users, the same

Table 2 PAPR level at CCDF= 10^{-3} .

		SC-FDMA				OFDMA	
α		0	0.25	0.5	0.75	1	
PAPR(dB)	QPSK	7.10	5.06	3.37	3.37	3.59	9.98
	16QAM	7.90	6.76	6.46	6.86	7.20	9.77





Fig. 4 PER peformance.

number of users can be accommodated. The throughput η (bps/Hz) is defined as

$$\eta = N \times R \times N_t \times \frac{1}{\bar{Q}} \times \frac{1}{1 + N_g/N_c},\tag{42}$$

where $\bar{Q}-1$ is the average number of packet retransmissions and N represents the number of bits per symbol.

The throughput performance with IC is plotted as a function of the average received E_s/N_0 in Fig. 5. Two cases of the decay factor β are considered: 0 dB (corresponding to the uniform power delay profile) and 3 dB. For comparison, the throughput performance of OFDMA with IAI cancellation is also plotted assuming M = 64 subcarriers, IFFT size $N_c = 256$, and GI size $N_g = 32$. In both SC-FDMA and OFDMA, bit interleaving is used after turbo encoding and puncturing to transform the burst errors into random errors.

At first, the case of β =0 dB (corresponding to the uniform power delay profile) is discussed. It can be seen from Fig. 5 that with MMSED-IC, α =1 provides higher throughput than α =0 over a wide E_s/N_0 region. Larger throughput

improvement is seen when higher coding rate (R = 3/4) is used. In this case, the coding gain is smaller, but larger frequency diversity gain is obtained. SC-FDMA using $\alpha = 1$ provides higher throughput than OFDMA which has no frequency diversity gain. Next, the case of $\beta=3$ dB is discussed. In this case, larger throughput performance improvement over OFDMA is seen than the case of $\beta=0$ dB. This is beccause OFDMA obtains smaller coding gain while SC-FDMA obtains relatively larger frequency diversity gain.

The peak E_s/N_0 is an important design parameter which determines the required peak transmit power of terminal transmitter power amplifiers. The throughput performance is plotted as a function of peak E_s/N_0 in Fig. 6 for the case of the decay factor $\beta=0$ (corresponding to the uniform power delay profile). The peak E_s/N_0 = is defined as peak E_s/N_0 = average received E_s/N_0 + PAPR_{0.1%} [16]. It can be seen from Fig. 6 that the throughput improvement is more pronounced due to the reduced PAPR. The throughput when $\alpha=1$ shows the highest over a wide E_s/N_0 region.



Fig. 5 Throughput vs. average received E_s/N_0 .

5. Conclusion

In this paper, we proposed an iterative MMSE detection and interference cancellation (MMSED-IC) scheme for uplink SC-FDMA MIMO using frequency-domain root Nyquist transmit filtering. By using a transmit filter with roll-off factor $\alpha > 0$, the adjacent users' spectra overlap with the desired signal spectrum and MUI occurs, to deal with the MUI, MUI&IAI&ISI cancellation is performed iteratively at the receiver. The PAPR, PER and throughput performances of the proposed schemes were evaluated by computer simulation. MMSED-IC can improve the PER performance while it can sufficiently suppress MUI&IAI&ISI. We showed that $\alpha = 1$ can achieve better PER performance compared to $\alpha = 0$ while sufficiently suppressing MUI, the additional frequency-diversity gain can be obtained by exploiting the excess bandwidth introduced by the transmit filtering. The throughput performance when $\alpha = 1$ is also higher than when $\alpha = 0$ as well as OFDMA over a wide E_s/N_0 region since larger frequency diversity gain is obtained. The throughput improvement is more pronounced when the throughput performance vs. peak E_s/N_0 is considered.

In a real system, the channel estimation error is present and degrades the HARQ throughput performance when using the proposed iterative MMSED-IC. Therefore, the impact of the channel estimation error on the throughput aachievable by the proposed scheme is practically important and is left as an future study.

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Fig. 6 Throughput vs. peak E_s/N_0 .

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