

# Adaptive Code Assignment Algorithm for A Multi-user/Multi-rate CDMA System

Qiyue YU<sup>†</sup> Le LIU<sup>‡</sup> and Fumiyuki ADACHI<sup>‡</sup>

<sup>†</sup> Harbin Institute of Technology, Harbin, China

<sup>‡</sup> Dept. of Electrical and Communication Engineering, Graduate School of Engineering, Tohoku University, 6-6-05  
 Aza-Aoba, Aramaki, Aoba-ku, Sendai, 980-8579 Japan

E-mail: <sup>†</sup> yuqiyue@gmail.com, <sup>‡</sup> l-liu@bp.jp.nec.com; adachi@ecei.tohoku.ac.jp

**Abstract** In this paper, we present a new adaptive code assignment algorithm. It has three main steps: reserved-space step, improved-crowded-first-space step, and multicode combination step. Compared with the existing algorithms, the proposed algorithm provides lower total blocking while its computational complexity is also comparatively low. It is applicable to all combinations users rate ratio probability. As a result, the proposed algorithm can be used in a multi-user/multi-rate CDMA system.

**Keyword** code assignment, CDMA, DCA, code tree, cost function

## 1. Introduction

In next generation mobile communications, a flexible support of multi-rate for multimedia services is required [1], [2]. Code division multiple access (CDMA) technique is used widely to solve this problem through changing the orthogonal spreading codes. The well-known CDMA techniques include single-carrier direct sequence DS-SS [2], [3] using time-domain spreading and multi-carrier MC-SS using frequency-domain spreading. Recently, the frequency-domain equalization (FDE) based on the minimum mean square error (MMSE) criterion has significantly improved the BER performance in a severe frequency-selective fading channel [2][4].

How to deal with the code assignment for multi-rate multi-user transmission is a serious problem. As is known, in OVSF CDMA, higher data rates are provided by using lower spreading factor. When a code is used in the OVSF code tree, its descendant and ancestor codes cannot be used [6]. This is because any two codes belonging to the same mother code are not orthogonal to each other. Therefore, the OVSF code tree has a limited number of available codes [7]. Since the maximum number of OVSF codes is limited, the efficient assignment of OVSF codes has a significant impact on the resource utilization. When old users leave and a new user arrives, the reassignment of OVSF codes should be efficiently done.

Recently, many researchers have been focusing on the code reassignment problem. In [8]~[12], various code assignment algorithms, such as random, leftmost, crowded-first-space, crowded-first-code, non-rearrangeable compact assignment(NCA)algorithms, have been proposed to find an optimum code to be assigned to a new comer. However, code-reassignment was not considered. In [13], [14], a dynamic code assignment (DCA) to reduce the blocking probability is presented, which is optimal in the sense that the number of OVSF codes that must be reassigned to support a new user, is minimized. However, these algorithms are very computationally complex [13]. Recently, less complex algorithms were proposed [15], [16]. These algorithms are a kind of static code assignment algorithm. But they are not very flexible compared with DCA and provide a relative high blocking

probability since it does not consider the rate distribution. An interesting code assignment algorithm is a hybrid algorithm that combines a DCA algorithm with a static algorithm [17]~[19]. However, the hybrid algorithms in [17]~[19] do not consider the dynamic and static code space boundary clearly.

This paper focuses on the hybrid code assignment algorithm for a multi-rate/multi-user CDMA system. The remainder of the paper is organized as follows. Section 2 reviews the OVSF code tree and multi-code spreading. Then the paper will introduce the adaptive code assignment algorithm in Sect. 3. In Sect. 4, the simulation results for the blocking probability will be presented and discussed. Finally, Section 5 offers some concluding remarks.

## 2. Preliminary

### 2.1. OVSF code tree

OVSF codes can be represented by a code tree as shown in Fig.1.

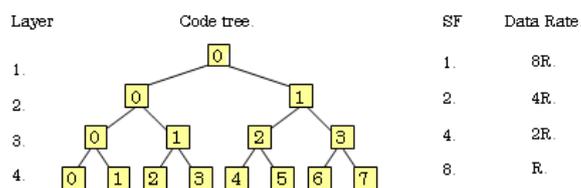


Fig.1 OVSF code tree.

Each OVSF code is denoted as  $C_{p,k}$ , where  $p$  represents the code layer of Walsh spreading codes and  $k$  ( $0, 1, \dots, 2^{p-1}-1$ ) represents the index of spreading code in layer  $p$ . The root code is  $C_{1,0}=(1)$  and the second layer has two codes,  $C_{2,0}=(1,1)$  and,  $C_{2,1}=(1,-1)$ . The codes at the  $p$ th layer are generated as  $(C, C)$  and  $(C, \bar{C})$  from each code  $C$  of the  $(p-1)$ th layer, where  $\bar{C}$  is the bit-wise complement of  $C$ [8]. The number of codes available at each layer is determined by the spreading factor  $SF$  of the layer. All codes in the same layer are orthogonal while codes in



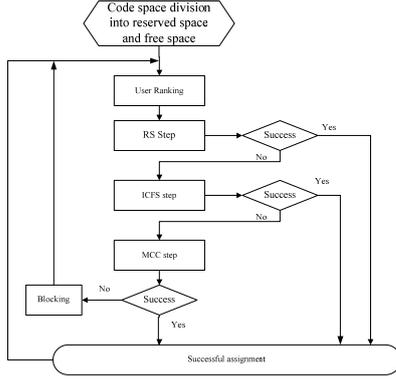


Fig.5 ACA algorithm.

### 3.2. Reserved-space step (RS)

$R$  is the data rate supported by a leaf code. The code tree consists of  $C_{SF}$  leaves. In a code-limited single-cell case, the maximum system capacity is equal to  $C_{SF}$ . Since all codes are mutually orthogonal, there is no multiple access interference [13]. Thus, if the total number of users in the system is denoted by  $L$  and the rate of user  $i$  is denoted by  $k_i R$ , the following should be satisfied.

$$\sum_{i=1}^L k_i \leq C_{SF} \quad (1)$$

The code assignment is based on Eq. (1). Divide the whole space into two: the reserved space and free space. Denote the rate distribution of  $(8R, 4R, 2R, R)$  by  $(P_{8R}, P_{4R}, P_{2R}, P_R)$  with

$$P_{8R} + P_{4R} + P_{2R} + P_R = 1 \quad (2)$$

Create a reserved space of  $(1-Q)$  times total capacity ( $0 \leq Q \leq 1$ ).

The number  $N$  of supportable users in the reserved space is given by

$$N = \left\lfloor \frac{C_{SF} \times (1-Q)}{P_{8R} \times 8 + P_{4R} \times 4 + P_{2R} \times 2 + P_R \times 1} + 0.5 \right\rfloor \quad (3)$$

Therefore, the distribution of supportable users of different rates is given by

$$\begin{cases} N_{8R} = \lfloor NP_{8R} + 0.5 \rfloor \\ N_{4R} = \lfloor NP_{4R} + 0.5 \rfloor \\ N_{2R} = \lfloor NP_{2R} + 0.5 \rfloor \\ N_R = \lfloor NP_R + 0.5 \rfloor \end{cases} \quad (4)$$

The reserved space capacity is given by

$$C_{RS} = N_{8R} \times 8 + N_{4R} \times 4 + N_{2R} \times 2 + N_R \times 1 \approx C_{SF} \times (1-Q) \quad (5)$$

The free space capacity is given by

$$C_{FS} = C_{SF} - C_{RS} \approx C_{SF} \times Q \quad (6)$$

Below an example is given to show how the reserved space is created. Assume  $C_{SF}=32$  and the user rate distribution of  $(8R, 4R, 2R, R)=(0.25, 0.25, 0.25, 0.25)$ . When  $Q=0.5$ , we have

$$\begin{aligned} N &= \left\lfloor \frac{32 \times (1-0.5)}{0.25 \times 8 + 0.25 \times 4 + 0.25 \times 2 + 0.25 \times 1} + 0.5 \right\rfloor \\ &= \left\lfloor \frac{32 \times (1-0.5)}{3.75} + 0.5 \right\rfloor = 4 \end{aligned} \quad (7)$$

$$\begin{cases} N_{8R} = \lfloor NP_{8R} + 0.5 \rfloor = \lfloor 4 \times 0.25 + 0.5 \rfloor = 1 \\ N_{4R} = \lfloor NP_{4R} + 0.5 \rfloor = \lfloor 4 \times 0.25 + 0.5 \rfloor = 1 \\ N_{2R} = \lfloor NP_{2R} + 0.5 \rfloor = \lfloor 4 \times 0.25 + 0.5 \rfloor = 1 \\ N_R = \lfloor NP_R + 0.5 \rfloor = \lfloor 4 \times 0.25 + 0.5 \rfloor = 1 \end{cases} \quad (8)$$

$$\begin{cases} C_{RS} = N_{8R} \times 8 + N_{4R} \times 4 + N_{2R} \times 2 + N_R \times 1 = 15 \\ C_{FS} = C_{SF} - C_{RS} = 32 - 15 = 17 \end{cases} \quad (9)$$

The resultant code distribution in each layer is shown in Table 1.

Table 1 Code distribution

Layer	Reserved Space	Free Space
2, rate=8R	0	1~3
3, rate=4R	2	3~7
4, rate=2R	6	7~15
5, rate=R	14	15~31

Fig.6 shows this example. Black color represents the reserved code place, and white color means forbid place; grey color stands for the free space.

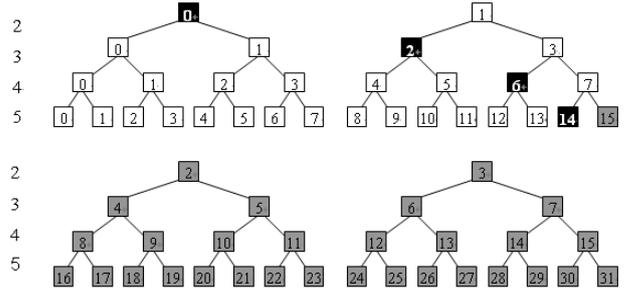


Fig.6 Code distribution space.

### 3.3. Improved-Crowded-First-Space (ICFS) Step

In the reserved space, we only need to find an appropriate code according to each user's rate. Unlike the RS step, however, the ICFS step ranks the incoming users in the ascending (from low to high) order of rate. A lower rate user assigned a code first since the number of lower rate codes is larger and consequently to reduce the total blocking probability. This is the difference of the ICFS from the original crowded-first-space [8] algorithm. The ICFS step is described below.

(a) Check if the free-space has enough capacity. If so, go to (b), otherwise go to MCC step.

(b) Pick the candidate code whose ancestor code has the least free capacity. Compare the free capacities of their ancestors. The one with less free capacity (i.e., more crowded) will be chosen for use. If two ancestors have the same free capacity, follow the leftmost strategy to pick the code on the left-hand side.

### 3.4. Multi-Codes Combination (MCC) Step

After carrying out the RS step and ICFS step, if some users with higher rate still do not have been assigned a code, this step is used.

If the system has enough remaining capacity to accommodate a user, then assign the multiple codes according to the multi-code combination. The reason for carrying out the MCC step last is that the multi-code transmission increases the peak-to-average power ratio (PAPR) of the transmit signal and a linear power amplifier with wide dynamic range is required and this is a problem for implementing low cost mobile terminals.

So far, we have described the proposed ACA algorithm.

## 4. Simulation results

A computer simulator will be implemented to evaluate the performance of the proposed algorithm. The maximum SF is set to 128. New calls arrive in a Poisson process with lambda value from 1 to 16, and the rates are R, 2R,

4R, 8R which rates ratio shown as Table 2. Call duration time is exponentially distributed with a mean of 3 time units. Traffic load decided by the coming users' number and their packet duration time.

Table 2 Simulation conditions

Maximum SF	128
Users Distribution	Poisson Distribution, Lambda = 1~16
User rates	R, 2R, 4R, 8R
Rates ratio (8R:4R:2R:R)	0.1:0.4:0.4:0.1 0.25:0.25:0.25:0.25 0.1:0.1:0.4:0.4 0.4:0.1:0.1:0.4
Duration	Exponential distribution. Mean= 3.

## 4.1. Compare with other algorithms

### 4.1.1 Comparison of blocking probabilities

First, the code blocking probability of the proposed ACA algorithm is compared with other algorithms as shown in Fig. 7. It can be observed that given the condition that when the system capacity can afford the traffic load (when the traffic load is lower than the available capacity), code blocking with not happen when using ACA or DCA algorithms. However, code blocking happens to Random algorithm and Crowded-first space algorithm with increasing probability when the traffic load increases.

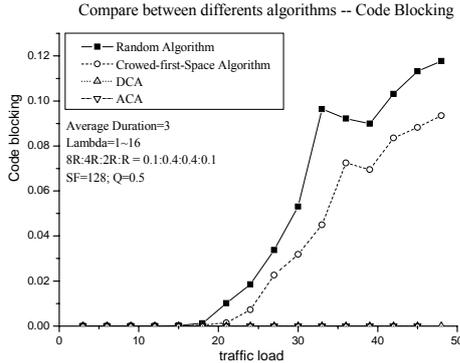


Fig.7 Code blocking

Furthermore, the proposed ACA algorithm outperforms the DCA algorithm when the total blocking is considered. The total blocking comparison between ACA algorithm and other algorithms is shown in Fig. 8. It is shown that the performance of the ACA algorithm is the best when compared to the other algorithms.

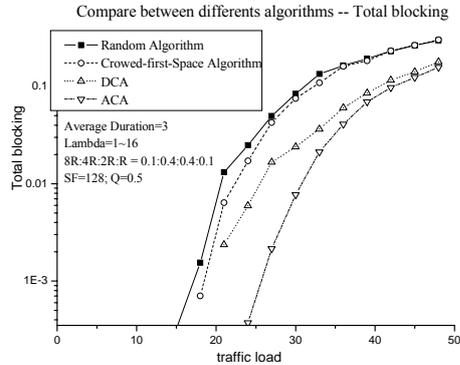


Fig.8 Total Blocking compare with other algorithms

### 4.1.2 Comparison of complexity

Complexity is an important factor to evaluate the performance of different algorithms. For easily, here define once do one time comparison, or once sum the capacity, or move the code to one place, the complexity will increase one. The complexities can be roughly calculated according to the value of SF, the ratio of different rates, the number of users as well as the code assignment algorithms.

$$N_{complex} \approx L \cdot P_{8R} \cdot \frac{SF}{8} + L \cdot P_{4R} \cdot \frac{SF}{4} + L \cdot P_{2R} \cdot \frac{SF}{2} + L \cdot P_R \cdot SF \quad (10)$$

The complexity of DCA algorithm is calculated as [13]

$$N_{complex} \approx L \cdot P_{8R} \cdot \left( \frac{SF}{8} \times 2 + \frac{1}{2} \cdot \frac{SF-8}{4} \times 2 + \frac{1}{2} \cdot \frac{SF-8-4}{2} \times 2 + \frac{1}{2} \cdot \frac{SF-8-4-2}{1} \right) + L \cdot P_{4R} \cdot \left( \frac{SF}{4} \times 2 + \frac{1}{2} \cdot \frac{SF-4}{2} \times 2 + \frac{1}{2} \cdot \frac{SF-4-2}{1} \right) + L \cdot P_{2R} \cdot \left( \frac{SF}{2} \times 2 + \frac{1}{2} \cdot \frac{SF-2}{1} \right) + L \cdot P_R \cdot SF \quad (11)$$

The complexity of the crowded-first-space algorithm [8] expresses as Eq. (12).

$$N_{complex} \approx L \cdot P_{8R} \cdot \left( \frac{SF}{8} \times 2 \right) + L \cdot P_{4R} \cdot \left( \frac{SF}{4} \times 2 \right) + L \cdot P_{2R} \cdot \left( \frac{SF}{2} \times 2 \right) + L \cdot P_R \cdot SF \quad (12)$$

Finally, the complexity of the proposed ACA algorithm is denoted in Eq. (13).

$$N_{complex} \approx (1-Q) \cdot (L \cdot P_{8R} \cdot N_{8R} + L \cdot P_{4R} \cdot N_{4R} + L \cdot P_{2R} \cdot N_{2R} + L \cdot P_R \cdot N_R) + Q \cdot \left[ L \cdot P_{8R} \cdot \left( \frac{SF}{8} \times 2 \right) + L \cdot P_{4R} \cdot \left( \frac{SF}{4} \times 2 \right) + L \cdot P_{2R} \cdot \left( \frac{SF}{2} \times 2 \right) + L \cdot P_R \cdot SF \right] + \frac{1}{3} \cdot (L \cdot P_{8R} \cdot \frac{SF}{8} + L \cdot P_{4R} \cdot \frac{SF}{4} + L \cdot P_{2R} \cdot \frac{SF}{2} + L \cdot P_R \cdot SF) \quad (13)$$

According to (10)~(13), the complexities of these algorithms are listed in Table 3.

Table 3

Complexities of different code assignment algorithms

Algorithm	Random	Crowded-first-space	DCA	ACA
Complexity	52.8L	92.8L	181.7L	67.4L

while  $L$  is the number of users.

Through the comparisons between the blocking probabilities and complexities, it is found that the proposed algorithm can achieve the best performance but with a relatively low complexity.

## 4.2. Characteristics of the ACA algorithm

### 4.2.1 Effect of rate ratio on the total blocking

The effect of the rate ratio on the average total blocking probability and the total blocking probabilities of different rates are considered first, as shown in Fig. 9 and Fig. 10, respectively.

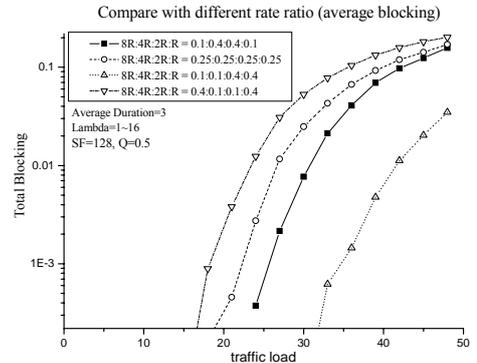


Fig.9 average blocking for different rate ratio

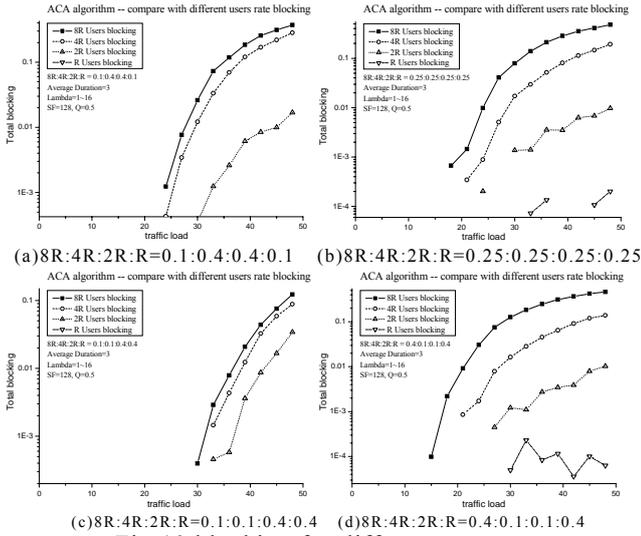


Fig.10 blocking for different user rate

It is shown that the more the lower-rate users are, the lower the total blocking probability is. In addition, the improvement gained by the lower rates is more significant. The reason behind is straight forward.

#### 4.2.2 The effect of Q on the blocking

Next, the effect of the value of Q, which represents the ratio between reserved space and free space, on the blocking probabilities will be studied. The effects of Q on the average total blocking and on the total blocking corresponding to different rates are shown in Fig. 11 and Fig. 12, respectively.

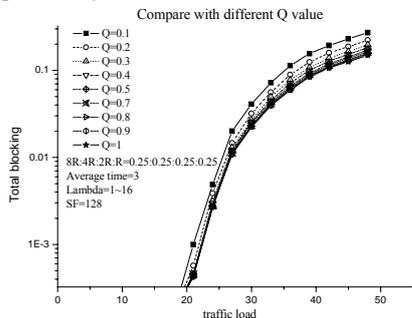


Fig.11 Average total blocking for different Q

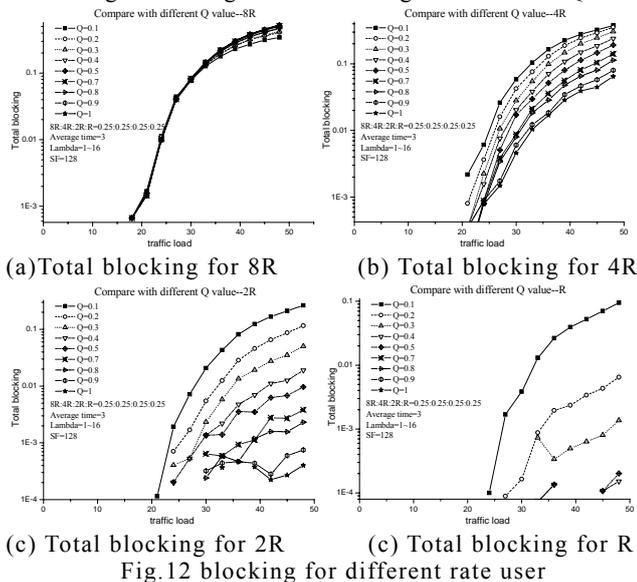


Fig.12 blocking for different rate user

An improvement of the average total blocking probability can be observed when Q increases. However, the effects of Q on different user rates are different. It is shown that the improvement on the low-rates is more significant (the total blocking probability corresponding to rate R reduces to 0 when Q exceeds 0.5). However the blocking of users with higher rate (8R) will become larger, and the complexity will increase as the increment of Q. Generally, if the probability of users with lower rate is higher, the Q should be larger; while the probability of users with higher rate increasing, the Q smaller is better.

## 5. Conclusions

This paper has proposed an adaptive code assignment algorithm for OVFS CDMA system. This algorithm performs the code assignment adaptively according to the user rates. It has been shown by the simulation results that the proposed algorithm can improve the total blocking probability significantly but with comparatively low complexity.

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